

The Heats of Formation of Diazene, Hydrazine, $N_2H_3^+$, $N_2H_5^+$, N_2H , and N_2H_3 and the Methyl Derivatives CH_3NNH , CH_3NNCH_3 , and $CH_3HNNHCH_3$

Myrna H. Matus, Anthony J. Arduengo, III, and David A. Dixon*

Chemistry Department, The University of Alabama, Shelby Hall, Box 870336, Tuscaloosa, Alabama 35487-0336

Received: March 24, 2006; In Final Form: June 5, 2006

The heats of formation of N_2H , diazene (*cis*- and *trans*- N_2H_2), N_2H_3 , and hydrazine (N_2H_4), as well as their protonated species (diazonium, $N_2H_3^+$, and hydrazinium, $N_2H_5^+$), have been calculated by using high level electronic structure theory. Energies were calculated by using coupled cluster theory with a perturbative treatment of the triple excitations (CCSD(T)) and employing augmented correlation consistent basis sets (aug-cc-pVnZ) up to quintuple- ζ , to perform a complete basis set extrapolation for the energy. Geometries were optimized at the CCSD(T) level with the aug-cc-pVDZ and aug-cc-pVTZ basis sets. Core-valence and scalar relativistic corrections were included, as well as scaled zero point energies. We find the following heats of formation (kcal/mol) at 0 (298) K: $\Delta H_f(N_2H) = 60.8$ (60.1); $\Delta H_f(cis-N_2H_2) = 54.9$ (53.2); $\Delta H_f(trans-N_2H_2) = 49.9$ (48.1) versus $\geq 48.8 \pm 0.5$ (exptl, 0 K); $\Delta H_f(N_2H_4) = 26.6$ (23.1) versus 22.8 ± 0.2 (exptl, 298 K); $\Delta H_f(N_2H_3) = 56.2$ (53.6); $\Delta H_f(N_2H_3^+) = 231.6$ (228.9); and $\Delta H_f(N_2H_5^+) = 187.1$ (182.7). In addition, we calculated the heats of formation of CH_3NH_2 , CH_3NNH , and $CH_3HNNHCH_3$ by using isodesmic reactions and at the G3(MP2) level. The calculated results for the hydrogenation reaction $RNNR + H_2 \rightarrow RHNNHR$ show that substitution of an organic substituent for H improved the energetics, suggesting that these types of compounds may be possible to use in a chemical hydrogen storage system.

Introduction

We have been exploring the thermodynamics of various compounds that could be used in chemical hydrogen storage systems either as compounds themselves or as intermediates in various approaches to store H_2 in a chemical compound for use in the transportation sector. We have been using high level ab initio molecular orbital theory to predict the heats of formation of relevant compounds based on an approach developed over a number of years at the Pacific Northwest National Laboratory. For example, we have studied borane amines¹ as well as related isoelectronic species² and carbenes.³ We are interested in organic derivatives of diazene or diimide (N_2H_2) and hydrazine (N_2H_4) as potential hydrogen storage systems based on cyanocarbon chemistry. For example, we are interested in the following generic reaction for different R groups:



We need to be able to predict the energetics for these species as well as for the addition of a proton to them and for the loss of H (breaking an N–H bond). We have already reported high level calculations on the various NH_x species, $x = 1$ to 3, and found excellent agreement with experiment.⁴ Our goal is to be able to predict the heats of formation of these compounds and then to use these results to develop heats of formation of larger organic derivatives based on isodesmic reactions.

Diazene is the prototypical azo-compound and its different isomers have been studied by using coupled cluster methods with large basis sets.^{5,6} Martin and Taylor used basis sets up through aug-cc-pV5Z to predict the heat of formation to be 49.2 ± 0.3 kcal/mol at 0 K at the CBS limit by using a calculated

anharmonic force field⁷ and including core-valence correlation corrections. This is in excellent agreement with the experimental value of $\geq 48.8 \pm 0.5$ kcal/mol.⁸ They also calculated the *cis*–*trans* isomerization energy to be 5.2 ± 0.2 kcal/mol at 0 K.

In recent years, computational approaches based on ab initio electronic structure theory have been used to reevaluate the heats of formation in small molecules in order to improve the accuracy of these values. We have used a composite theoretical approach, based on ab initio molecular orbital theory, in which empirical parameters are not included, except when necessary for spin–orbit energies in atoms and in calculating zero point energies.^{9,10} Our approach is based on calculating the total atomization energy (TAE) of a molecule to obtain heats of formation at 0 K utilizing the known heats of formation of the atoms. The TAE is calculated by using coupled cluster theory, including a perturbative treatment of the triple excitations (CCSD(T))^{11–13} combined with augmented correlation-consistent basis sets^{14,15} extrapolated to the complete basis set (CBS) limit to treat the correlation energy of the valence electrons. Corrections, such as core-valence interactions and relativistic effects, and the zero point energy (ZPE), obtained either from a combination of experiment and theory or from theoretical scaled values, are also included. The standard heats of formation of compounds at 298 K can then be calculated by using standard thermodynamic and statistical mechanics expressions.¹⁶

We have used such an approach to calculate the heats of formation of N_2H_2 , N_2H_4 , N_2H_3 , N_2H , diazenium ($N_2H_3^+$), and hydrazinium ($N_2H_5^+$). In addition, we calculated the heats of formation at the G3(MP2) level.¹⁷ We have also calculated the heats of formation of RNNH, RNNR, and RHNNHR for R = CH_3 by using an isodesmic reaction approach at the density functional theory level¹⁸ with the B3LYP exchange–correlation functional¹⁹ and at the MP2/CBS level as well as by direct

* Address correspondence to this author. E-mail: dadixon@bama.ua.edu.

calculation at the G3(MP2) level. These values are then used to assess the hydrogenation energy of reaction 1 for R = CH₃.

Computational Approach

The augmented correlation consistent basis sets aug-cc-pVnZ ($n = D, T, Q, 5$) were used for most of the calculations,²⁰ and, for brevity, the basis set names are shortened to aVnZ. All of the current work was performed with the Gaussian03²¹ and MOLPRO²² programs.

We first describe highly accurate calculations based on the CCSD(T)/CBS extrapolations. The geometries were optimized at the frozen core CCSD(T) level by using the aVDZ and aVTZ basis sets. This level of calculation was also employed for the prediction of the harmonic vibrational frequencies of N₂H (nonlinear, C_s symmetry), N₂H₂ (cis and trans isomers), N₂H₄, and their protonated species. For N₂H₃, the geometry and frequencies were calculated at the CCSD(T)/aVDZ level. We could not get the frequency calculations to converge for linear N₂H (C_{∞v} symmetry), so the frequencies for this transition state were calculated with the B3LYP exchange-correlation functional at the density functional theory level.

For *trans*-N₂H₂ and N₂H₄, the calculated harmonic frequencies were averaged with the corresponding experimental values to calculate the ZPE correction.²³ For *trans*-N₂H₂, Martin and Taylor⁶ find a ZPE of 17.53 kcal/mol and our value is 17.42 kcal/mol suggesting that our approach will introduce a maximum error of ±0.4 kcal/mol for the compounds with more hydrogens. For the remaining molecules, there are no experimental values so the ZPEs were scaled by a factor obtained from the ratio of the averaged ZPE from a molecule with experimental values and the theoretical ZPE from the same molecule. For *cis*-N₂H₂, N₂H, and N₂H₃⁺, the ZPEs were scaled by 0.983, obtained from the ratio of the averaged ZPE and the CCSD(T)/aVTZ ZPE values for *trans*-N₂H₂. For the *cis*-N₂H₂ isomer, Martin and Taylor obtain a ZPE of 17.15 kcal/mol and we obtain 17.03 kcal/mol. For N₂H₃ and N₂H₅⁺, the scaling factor is 0.987 from the ratio of the averaged ZPE and the CCSD(T)/aVTZ ZPE values for N₂H₄.

The CCSD(T)/aVTZ geometries were used in single point CCSD(T)/aVQZ and CCSD(T)/aV5Z calculations. The CCSD(T) total energies were extrapolated to the CBS limit by using a mixed exponential/Gaussian function of the form

$$E(n) = E_{\text{CBS}} + A \exp[-(n-1)] + B \exp[-(n-1)^2] \quad (2)$$

with $n = 2$ (aVDZ), 3 (aVTZ), and 4 (aVQZ), as proposed by Peterson et al.²⁴ We also used the following expansion in $1/l_{\text{max}}$,²⁵ where l_{max} equals the highest angular momentum present in the basis set, to estimate the complete basis set limit using the aVQZ and aV5Z results:

$$E(l_{\text{max}}) = E_{\text{CBS}} + B/l_{\text{max}}^3 \quad (3)$$

The use of expressions 2 and 3 provides insight into the extrapolation error. The CCSD(T) calculations for open-shell atoms and molecules were carried out at the R/UCCSD(T) level. In this approach, a restricted open shell Hartree-Fock (ROHF) calculation was initially performed and the spin constraint was relaxed in the coupled cluster calculation.²⁶⁻²⁸

Core-valence corrections, ΔE_{CV} , were obtained at the CCSD(T)/cc-pwCVTZ level.²⁹ Scalar relativistic corrections, ΔE_{SR} , which account for changes in the relativistic contributions to the total energies of the molecule and the constituent atoms, were included at the CI-SD (configuration interaction singles and

TABLE 1: Comparison of Calculated Bond Lengths (Å) and Angles (deg) with Experimental Values

molecule	method	r_{NN}	r_{NH}	$\angle\text{NNH}$	$\angle\text{HNNH}$
N ₂	CCSD(T)/aVDZ	1.1209			
	CCSD(T)/aVTZ	1.1040			
	exptl ^a	1.0977			
NH ₃	CCSD(T)/aVTZ		1.0237	105.9 ^g	112.2 ^h
	CCSD(T)/aVTZ		1.0149	106.40 ^g	113.20 ^h
	exptl ^b		1.0116	106.7 ^g	113.7 ^h
N ₂ H (C _s)	CCSD(T)/aVDZ	1.1986	1.0607	115.60	
	CCSD(T)/aVTZ	1.1830	1.0517	116.44	
N ₂ H (C _{∞v})	CCSD(T)/aVDZ	1.1969	1.0079	180.00	
	CCSD(T)/aVTZ	1.1820	0.9982	180.00	
<i>cis</i> -N ₂ H ₂	CCSD(T)/aVDZ	1.2652	1.0464	111.57	0.0
	CCSD(T)/aVTZ	1.2526	1.0365	111.77	0.0
	CCSD(T)/aVDZ	1.2659	1.0415	105.75	180.0
<i>trans</i> -N ₂ H ₂	CCSD(T)/aVTZ	1.2528	1.0318	106.13	180.0
	CCSD(T) ^c	1.2468	1.0281	106.17	
	exptl ^d	1.247	1.029	106.3	
N ₂ H ₃	MP2/aVDZ	1.3496	1.0275	105.53	
			1.0132	113.91	167.84
			1.0171	120.86	23.97
	MP2/aVTZ	1.3393	1.0186	105.82	
			1.0056	114.21	168.11
			1.0092	120.93	22.92
	CCSD(T)/aVDZ	1.3683	1.0334	105.82	
			1.0170	112.45	165.47
			1.0210	119.00	29.02
N ₂ H ₃ ⁺	CCSD(T)/aVDZ	1.2476	1.0422	109.66	
			1.0330	116.95	180.00
			1.0359	124.53	0.00
	CCSD(T)/aVTZ	1.2346	1.0334	110.20	
			1.0260	117.13	180.00
			1.0286	124.46	0.00
N ₂ H ₄	CCSD(T)/aVDZ	1.4559	1.0222	106.15	154.58
			1.0252	110.85	-90.13
	CCSD(T)/aVTZ	1.4448	1.0130	106.63	153.79
			1.0162	111.13	-89.73
	exptl ^e	1.447(5)	1.008(8)	109.2(8)	88.9(15)
		1.447(2)	1.015(2)	106(2)	91(2)
N ₂ H ₅ ⁺	CCSD(T)/aVDZ	1.4605	1.0332	116.20	
			1.0288	107.31	±122.60
			1.0288	107.31	±57.39
	CCSD(T)/aVTZ	1.4509	1.0266	115.85	
			1.0212	107.56	±122.42
			1.0212	107.56	±57.94

^a Huber, K. P.; Herzberg, G. *Molecular Spectra and Molecular Structure Constants of Diatomic Molecules*; Van Nostrand-Reinhold: New York, 1979. ^b Duncan, J. L.; Mills, I. M. *Spectrochim. Acta* **1964**, *20*, 523. ^c Reference 5, CCSD(T)/cc-pvQZ+CCSD(T)/MTcore-CCSD(T)/MTnocore. ^d Reference 35. ^e ref 36a, microwave. ^f Reference 36b, microwave and electron diffraction. ^g $\angle\text{HNNH}$. ^h $\angle\text{HNNH}$.

doubles) level of theory by using the aug-cc-pVTZ basis set. ΔE_{SR} is taken as the sum of the mass-velocity and 1-electron Darwin (MVD) terms in the Breit-Pauli Hamiltonian.³⁰ For these species, there is no spin-orbit correction in the atoms.

The dissociation energy ($\sum D_0$ or TAE) of a compound is given by the expression:

$$\sum D_0 = \Delta E_{\text{elec}}(\text{CBS}) - \Delta E_{\text{ZPE}} + \Delta E_{\text{CV}} + \Delta E_{\text{SR}} \quad (4)$$

By following the procedures by Curtiss et al.,¹⁶ we can obtain gas phase heats of formation at 298 K from our computed $\sum D_0$ values and the known heats of formation at 0 K for the elements ($\Delta H_f^0(\text{N}) = 112.53$ kcal/mol and $\Delta H_f^0(\text{H}) = 51.63$ kcal/mol).³¹

For the molecules with R = CH₃, the geometries were optimized at the B3LYP/aVTZ level and frequencies for zero point and thermal corrections were also obtained at this level. MP2 calculations³² were done with this geometry with the aVnZ basis sets $n = D, T, \text{ and } Q$, and extrapolated to the CBS limit

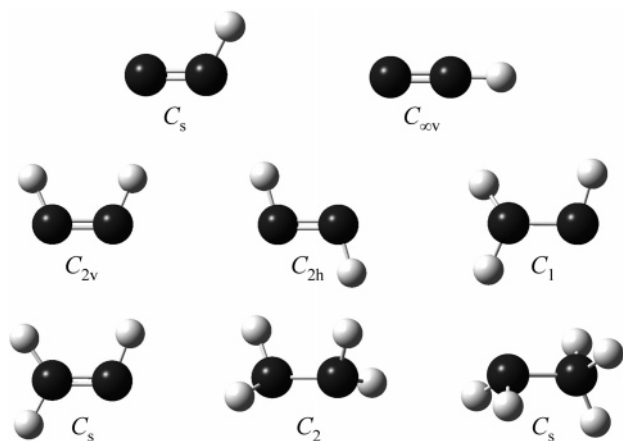
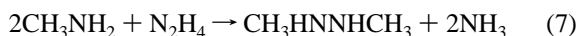
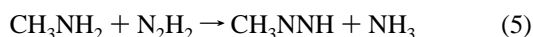


Figure 1. Optimized molecular structures and their symmetry point group for NH_2 (nonlinear), NH_2 (linear), *cis*- N_2H_2 , *trans*- N_2H_2 , N_2H_3 , N_2H_3^+ , N_2H_4 , and N_2H_5^+ .

by using eq 2. We then used the following isodesmic reactions to calculate the heats of formation.



We also calculated the isodesmic reaction energies at the DFT level with the B3LYP functional¹⁹ and the DZVP2³³ and 6-311++G**³⁴ basis sets. In addition, all of the heats of formation were calculated with the G3(MP2) approach.¹⁷

Results and Discussion

The geometry parameters of the N_2H_x compounds are given in Table 1 and the geometries and point group symmetries for the different species are shown in Figure 1. For *trans*- N_2H_2 , the geometry is in good agreement with the best computational values^{6,7} as well as the experimental values³⁵ within 0.005 Å with the aVTZ basis set. For N_2H_4 , there is similar good agreement with experiment³⁶ for the aVTZ geometry. The bond distance in N_2H_4 is much longer than the bond distance in N_2H_2 consistent with the nominal single bond character in the former and the nominal double bond character in the latter.

The geometry of N_2H is predicted to be bent as would be expected and has ${}^2A'$ symmetry. The linear structure is predicted to be a transition state for inverting the $\angle\text{NNH}$ and is 27.2 kcal/mol higher in energy at the CCSD(T)/CBS level. The geometry of N_2H shows an N–H bond elongated from that in *trans*- N_2H_2 and an N–N bond that is shorter than that in N_2H_2 by 0.07 Å but longer than that in N_2 by 0.08 Å at the aVTZ level. N_2H_3^+ is similar to N_2H_2 in that it has a reasonably short N–N bond. The molecule is planar and the short N–N bond is consistent with this as the molecule can be considered to be an amine

TABLE 2: Calculated and Experimental Vibrational Frequencies (cm^{-1})^a

molecule	symmetry	aVDZ	aVTZ	exptl	molecule	symmetry	aVDZ	aVTZ	exptl
N_2	σ_g	2318.3	2339.6	2331 ^b ($\omega_e = 2358.6$)	N_2H_3^+	a''	1059.5	1056.6	
NH_3	a_1		1063.7	950 ^c	a'	1195.1	1194.4		
	e		1671.1	1627 ^c	a''	1230.2	1239.0		
	a_1		3463.9	3337 ^c	a'	1491.6	1493.6		
	e		3592.5	3444 ^c	a'	1586.6	1593.0		
N_2H (C_s)	a'	1098.5	1108.1		a'	1733.2	1734.0		
	a'	1785.6	1802.6		a'	3321.4	3339.9		
	a'	2866.5	2891.3		a'	3337.7	3354.7		
N_2H ($C_{\infty v}$) ^f	π	1486.8i	1468.6i		a'	3472.6	3473.8		
	π	530.5	616.7		a	404.1	406.0		
	σ	1937.7	1933.8		a	841.7	840.7	780 ^g	
<i>cis</i> - N_2H_2	σ	3785.0	3802.5		b	1026.6	1020.0	966 ^h	
	a_2	1231.5	1247.9		a	1104.6	1114.0	1076 ^g	
	a_1	1351.2	1364.2		b	1292.7	1302.7	1275 ^h	
	b_2	1535.5	1553.9		a	1332.3	1338.7	1275 ^g	
	a_1	1554.3	1563.3		b	1651.2	1674.0	1628 ^h	
<i>trans</i> - N_2H_2	b_2	3108.9	3146.8		a	1665.3	1685.2	1642 ^g	
	a_1	3196.8	3232.0		b	3426.0	3460.0	3314 ^h	
	a_u	1305.5	1317.5	1288.6 ^d	a	3436.8	3469.0	3329 ^g	
	b_u	1334.1	1343.9	1316.4 ^d	a	3535.8	3563.8	3398 ^g	
	a_g	1547.1	1551.5	1529 ^e	b	3538.6	3569.0	3350 ^h	
	a_g	1604.3	1612.1	1583 ^e	a''	326.6	335.8		
N_2H_3	a_g	3233.2	3264.8	3128 ^e	a'	900.6	909.7	973	
	b_u	3263.3	3297.2	3120.3 ^d	a''	1045.6	1052.7	1246	
	a	606.3			a'	1054.3	1059.2	1101	
	a	708.9			a'	1209.8	1213.7	1124	
	a	1136.3			a''	1436.6	1448.1	1584	
	a	1213.4			a'	1531.5	1554.5	1417	
	a	1477.5			a'	1641.4	1663.9	1510	
	a	1646.7			a''	1655.4	1678.8	1638	
	a	3377.3			a'	1680.9	1699.6	1610	
	a	3471.9			a'	3355.4	3376.9	2716	
	3622.2			a'	3418.3	3434.1	2950		
				a''	3465.1	3480.5	3034		
				a'	3490.1	3506.5	3150		
				a''	3519.6	3532.1	3261		

^a All frequencies calculated at the CCSD(T) level except for N_2H which were obtained at the DFT level with the B3LYP exchange-correlation functional. ^b Huber, K. P.; Herzberg, G. *Molecular Spectra and Molecular Structure Constants of Diatomic Molecules*; Van Nostrand-Reinhold: New York, 1979. ^c Shimanouchi, T. *Tables of Molecular Vibrational Frequencies*; Consolidated Vol. 1, NSRDS NBS-39. ^d Reference 39. ^e Reference 38. ^f Reference 41. ^g Reference 40. ^h Reference 42. ⁱ References 37a and 44. ^j Broken symmetry solution for linear N_2H .

TABLE 3: Calculated Dissociation Energies at 0 K^a

molecule	CBS(2) ^b	CBS(3) ^c	ΔE_{ZPE}^d	ΔE_{CV}^e	ΔE_{SR}^f	$\Sigma D_0(2)^g$	$\Sigma D_0(3)^h$
N ₂	227.15	227.48	3.36	0.63	-0.12	224.31	224.63
NH ₃	297.45	297.48	21.09	0.34	-0.29	276.41	276.54
N ₂ H (C _s)	223.56	223.72	8.16 ⁱ	0.67	-0.27	215.81	215.97
N ₂ H (C _{∞v})	196.34	196.41	8.93 ⁱ	0.88	-0.35	187.93	188.01
<i>cis</i> -N ₂ H ₂	290.12	290.28	17.03 ⁱ	0.63	-0.34	273.37	273.53
<i>trans</i> -N ₂ H ₂	295.49	295.64	17.42	0.67	-0.36	278.38	278.54
N ₂ H ₃ ^j	347.64		24.38 ^k	0.98	-0.49	323.75	
N ₂ H ₃ ⁺	173.92		25.99 ⁱ	0.81	-0.41	148.34	
N ₂ H ₄	437.30	437.42	32.80	1.00	-0.54	404.96	405.08
N ₂ H ₅ ⁺	337.89		42.29 ^k	1.06	-0.55	296.12	

^a Results are given in kcal/mol. ^b Extrapolated by using eq 2 with $aVnZ$, where $n = D, T, \text{ and } Q$. ^c Extrapolated by using eq 3 with $aVQZ$ and $aV5Z$. ^d The zero point energies were obtained from the average of CCSD(T)/aVTZ and experimental values, when available, as reported in Table 2. See text for details. ^e Core/valence corrections were obtained with the cc-pwCVTZ basis sets at the CCSD(T)/aVTZ optimized geometries. ^f The scalar relativistic correction is based on a CISD/aVTZ calculation. ^g ΣD_0 computed with the CBS extrapolation obtained by using eq 2. ^h ΣD_0 computed with the CBS extrapolation obtained by using eq 3. ⁱ A scale factor of 0.983, obtained from *trans*-N₂H₂, was used. ^j For the ZPE, CCSD(T)/aVDZ values were used. ^k A scale factor of 0.987, obtained from N₂H₄, was used.

with an NH⁺ substituent. Highly electropositive substituents tend to lower the inversion barrier in amines consistent with the overall planar structure. In contrast, N₂H₃ has a nonplanar structure with a pyramidalized (HN)⁺NH₂ group and a N–N bond that is ~ 0.1 Å longer than the N–N bond in N₂H₃⁺. N₂H₅⁺ is similar to N₂H₄ with a long N–N single bond that is slightly lengthened from that in N₂H₄. The molecule can be described best as a protonated amine with a NH₂ substituent. The N–N bond distance in the ion is in reasonable agreement with the value of 1.44 Å from experiment.³⁷

The calculated vibrational frequencies are given in Table 2 and compared to experiment for N₂H₂ and N₂H₄. Martin and co-workers^{6,7} have done an excellent job on analyzing the results for N₂H₂ so we do not do so here, except to note that the computed harmonic values are larger than the experimental ones^{38,39} as expected, especially for the N–H stretches where the effects of anharmonicity are the largest.

Durig and co-workers⁴⁰ have assigned most of the vibrational frequencies for the a symmetry modes in N₂H₄ except for the lowest a mode that was obtained by Yamaguchi et al.⁴¹ The agreement is reasonable with the calculated harmonic values higher than the experimental ones which contain anharmonic contributions as expected. To evaluate the thermodynamic properties of N₂H₄, the frequencies of the b symmetry modes were estimated.⁴² On the basis of the comparison with the a symmetry modes, it is clear that the highest energy N–H stretching mode of b symmetry has been estimated to be too low. The remaining b symmetry modes are reasonable estimates based on comparison with the calculated values.

For N₂H (nonlinear), the N–H stretch is predicted to be lower than that in N₂H₂. The N–N bond stretch is predicted to be at 1803 cm⁻¹ in comparison to values for N₂ of 2340 cm⁻¹ with the aVTZ basis set and an experimental harmonic value of 2360 cm⁻¹.⁴³ For N₂H₃⁺, the N–N stretch at 1734 cm⁻¹ is higher than the stretch at 1612 cm⁻¹ (1583 cm⁻¹, experiment) calculated for *trans*-N₂H₂. The N–H stretches are predicted to be higher than those in N₂H₂ but not as high as those in N₂H₄. For N₂H₃, the N–N stretch is lower than those of *trans*-N₂H₂ and N₂H₃⁺, 1213 cm⁻¹ versus 1604 and 1733 cm⁻¹, respectively, at the CCSD(T)/aVTZ level. For N₂H₅⁺, the calculated N–N stretch (1059 cm⁻¹) is lower than that for N₂H₄ (1114 cm⁻¹, calculated; 1076 cm⁻¹, experiment⁴⁰).

The vibrational spectrum for N₂H₅⁺ has been reported⁴⁴ and analyzed by a force field approach.^{37a} We note that a number of assumptions were made in the symmetry assignments which are not correct so we prefer our ordering.

TABLE 4: CCSD(T) Calculated and Experimental Heats of Formation at 0 and 298 K (kcal/mol)^a

molecule	$\Delta H_f(0\text{K})^b$	$\Delta H_f(0\text{K})$		$\Delta H_f^0(298\text{K})^b$	
		exptl		exptl	
N ₂	0.6	0.0	0.6	0.0	
NH ₃	-9.1	-9.30 ± 0.10^c	-10.7	-10.98 ± 0.08^e	
N ₂ H (C _s)	60.8		60.1		
N ₂ H (C _{∞v})	88.7		87.8		
<i>cis</i> -N ₂ H ₂	54.9		53.2		
<i>trans</i> -N ₂ H ₂	49.9	$\geq 48.8 \pm 0.5^d$	48.1	$\geq 46.6 \pm 0.8^f$	
N ₂ H ₃	56.2		53.7		
N ₂ H ₃ ⁺	231.6		228.9		
N ₂ H ₄	26.6	26.2 ^c	23.1	22.8 ± 0.2^e	
N ₂ H ₅ ⁺	187.1		182.7		

^a Additional useful values: $\Delta H_f^0(\text{NH}) = 85.92$ kcal/mol, $\Delta H_f^0(\text{NH}_2) = 45.27$ kcal/mol, $\Delta H_f^0(\text{NH}_3) = -9.10$ kcal/mol at 0 K. $\Delta H_f^0(\text{NH}) = 85.94$ kcal/mol, $\Delta H_f^0(\text{NH}_2) = 44.58$ at 298 K. At 0 K, $\Delta H_f^0(\text{H}^+) = 365.22$ kcal/mol and at 298 K, $\Delta H_f^0(\text{H}^+) = 365.7$ kcal/mol. See refs 4 and 31. ^b The reported heats of formation were obtained by averaging $\Sigma D_0(2)$ and $\Sigma D_0(3)$ where available or using $\Sigma D_0(2)$ if that is the only available value. ^c Reference 31. ^d Reference 8. ^e Reference 45. ^f Reference 50.

The energy components used in calculating the total dissociation energy to atoms are given in Table 3 for use in eq 4. The values with the two extrapolation procedures are within 0.2 kcal/mol of each other, suggesting that the error in the extrapolation procedure is ± 0.2 kcal/mol. The core valence ΔE_{CV} corrections are modest ranging from 0.63 to 1.06 kcal/mol, and the scalar relativistic ΔE_{SR} corrections are somewhat smaller and of opposite sign ranging from -0.27 to -0.55 kcal/mol.

The predicted heats of formation are given in Table 4. We have included the values for N₂ and NH₃ for comparison. The calculated heat of formation for N₂ is too positive by 0.6 kcal/mol as compared to the experimental value.³¹ The calculated values for $\Delta H_f(\text{NH}_3)$ are in excellent agreement with the experimental values of 9.30 ± 0.10 kcal/mol³¹ at 0 K and 10.98 ± 0.08 kcal/mol⁴⁵ at 298 K. The calculated value for N₂H₂ is in excellent agreement with the experimental lower bound⁸ and the calculation of Martin and Taylor.⁶ The calculated heat of formation of N₂H₄ at 0 and 298 K is in excellent agreement with the experimental value³¹ at 0 K of 26.20 ± 0.2 kcal/mol and at 298 K of 22.8 ± 0.2 kcal/mol.

The N–H bond energy in N₂H₂ is 62.5 kcal/mol and in N₂H₄ it is 81.2 kcal/mol which can be compared to the respective N–H bond energies⁴ in NH₃, NH₂, and NH of 106.0, 92.3, and 78.2 kcal/mol, all at 0 K. Our calculations enable us to predict the N–N bond strengths. The N–N bond strength in N₂ is 225.1

TABLE 5: Entropies at 298 K (cal/(mol·K))

molecule	S(298K)	molecule	S(298K)
N ₂ H (C _s)	37.47 ^a	N ₂	45.78 ^a
<i>cis</i> -N ₂ H ₂	52.21 ^a	NH	41.06 ^a
<i>trans</i> -N ₂ H ₂	52.15 ^a	NH ₂	46.49 ^a
N ₂ H ₃	56.71 ^b	NH ₃	49.03 ^a
N ₂ H ₃ ⁺	54.32 ^a	CH ₃ NH ₂	57.53 ^d
N ₂ H ₄	55.17 ^a	CH ₃ NNH	61.83 ^d
N ₂ H ₅ ⁺	57.33 ^a	CH ₃ NNCH ₃	69.82 ^d
H ⁺	26.04 ^c	CH ₃ HNNHCH ₃	71.88 ^d
H ₂	31.13 ^a		

^a CCSD(T)/aVTZ. ^b CCSD(T)/aVDZ. ^c Experimental value, ref 31. ^d B3LYP/aVTZ.

kcal/mol (nominal triple bond).⁴³ The N–N bond strength in HNNH is 121.9 kcal/mol (nominal double bond) and it is 63.9 kcal/mol in H₂NNH₂ (nominal single bond).

The proton affinity of N₂H₂ is 184.9 kcal/mol in comparison to a value of 192 kcal/mol at 298 K from a low level CISD/6-31G**//6-31G** calculation.⁴⁶ The older value is in error by about 7 kcal/mol as compared to our more reliable value. This result shows that NH⁺ substitution for H reduces the proton affinity^{47,48} of NH₃ by about 20 kcal/mol. The calculated proton affinity of N₂H₄ is 206.1 kcal/mol in comparison to an experimental value of 203.9 kcal/mol at 298 K.⁴⁷ The ionization energy of N₂H₃ is predicted to be 7.59 eV.

Molecular entropies are given in Table 5. The theoretical energetics for some simple hydrogenation reactions are given below (using a calculated value of $\Delta H_f(\text{H}_2) = -0.1$ kcal/mol at 298 K).



$$\Delta H(298\text{K}) \text{ kcal/mol} = 47.6; \Delta G(298\text{K}) = 55.0 \text{ kcal/mol}$$



$$\Delta H(298\text{K}) = -24.9 \text{ kcal/mol}; \Delta G(298\text{K}) = -16.5 \text{ kcal/mol}$$

As expected, hydrogenation of N₂ (reaction 8) is an endothermic process whereas hydrogenation of N₂H₂ (reaction 1a) is an exothermic process. Hydrogenation of N₂H₄ to form two NH₃ molecules (reaction 9) is also an exothermic process and the values of the enthalpy and free energy are comparable. The experimental value of -44.8 kcal/mol for $\Delta H(298\text{K})$ for reaction 9 is in excellent agreement with our calculated value.



$$\Delta H(298\text{K}) = -44.4 \text{ kcal/mol}; \Delta G(298\text{K}) = -47.9 \text{ kcal/mol}$$

To estimate the heats of formation for CH₃NNH, CH₃NNCH₃, and CH₃HNNHCH₃, we calculated the energy of the isodesmic

reactions 5–7 and used the experimental values for CH₃NH₂ (-1.9 kcal/mol at 0 K and -5.4 kcal/mol at 298 K)⁴⁹ and NH₃ (-9.30 kcal/mol at 0 K and -10.98 kcal/mol at 298 K),³¹ and our computed values for N₂H₂ and N₂H₄. The results for the reaction energies are given in Table 6. The differences in the minimum and maximum values for each of reactions 5, 6, and 7 are 1.2, 2.9, and 3.9 kcal/mol, respectively. The DFT values are consistently lower than the MP2 values. There is not a large basis set dependence for either the DFT or MP2 calculations, both less than 1 kcal/mol. To calculate the heats of formation, we used the MP2/CBS values with the results given in Table 7.

We also calculated the heats of formation at the G3(MP2) level¹⁷ as given in Table 7. We see that for all of the compounds, the G3(MP2) method gives heats of formation that are too positive for NH₃, CH₃NH₂, N₂H₂, and N₂H₄. Thus the G3(MP2) heats of formation for the methyl derivatives are too positive as compared to our isodesmic reaction values because the energetics of the underlying base structures are too positive.

Our heats of formation for the methyl derivatives allow us to predict the hydrogenation energy of the following reaction:



$$\Delta H(298\text{K}) = -13.8 \text{ kcal/mol}; \Delta G(298\text{K}) = -5.1 \text{ kcal/mol}$$

We note that the introduction of methyl groups makes the reaction substantially less exothermic demonstrating that we can design an organic reaction that will have the appropriate substituents to make the reaction more thermoneutral. This will be critical for chemical hydrogen storage systems which need to be near thermoneutral to minimize the energy needed to liberate the hydrogen and to regenerate the storage material.

Conclusion

The heats of formation of N₂H_x compounds were calculated by using ab initio molecular orbital theory at the CCSD(T)/CBS level. Our calculated results are in very good agreement with the available experimental values. These values were used to calculate ionization energies, proton affinities, bond energies, and hydrogenation energies. We calculated the heats of formation of N₂(H)_x(CH₃)_y molecules by using an isodesmic reaction approach with reaction energies calculated at the MP2/CBS level. We also calculated the heats of formation of the N₂H_x and the N₂(H)_x(CH₃)_y molecules at the G3(MP2) level. The G3(MP2) heats of formation for the N₂H_x molecules are higher in energy than those obtained with the CCSD(T)/CBS procedure and are not in as good agreement with the experiment. The calculated results for the hydrogenation reactions show that substitution of an organic substituent for H improves the

TABLE 6: Comparison of Calculated Enthalpies (kcal/mol) for Reactions 5, 6, and 7^a

level of calculation	$\Delta E(\text{OK})$			$\Delta H^0(298\text{K})$		
	reaction 5	reaction 6	reaction 7	reaction 5	reaction 6	reaction 7
B3LYP/DGDZVP2	-10.99	-20.61	-8.13	-11.54	-21.94	-9.44
B3LYP/6-311++G**	-10.56	-19.97	-8.23	-11.15	-21.35	-9.58
B3LYP/aVDZ	-10.66	-20.09	-8.43	-11.30	-21.59	-9.83
B3LYP/aVTZ	-10.90	-20.64	-8.39	-11.51	-22.09	-9.79
MP2/aVDZ	-11.46	-22.33	-12.04	-12.07	-23.78	-13.44
MP2/aVTZ	-11.73	-22.84	-11.65	-12.34	-24.29	-13.05
MP2/aVQZ	-11.64	-22.67	-11.44	-12.26	-24.11	-12.84
MP2/CBS(1) ^b	-11.57	-22.53	-11.31	-12.19	-23.98	-12.71
G3(MP2) ^c	-10.83	-21.06	-11.22	-11.40	-22.41	-12.40

^a The thermal corrections to the enthalpies at the MP2 level for calculating $\Delta H^0(298\text{K})$ were taken from B3LYP/aVTZ calculations. ^b MP2/CBS(1) + ZPE (B3LYP/aVTZ) = $\Delta H^0(\text{OK})$: -12.39 (reaction 5), -24.70 (reaction 6), -13.37 (reaction 6) kcal/mol. ^c G3(MP2) values at 0 K do not include ZPE, the corresponding values with ZPE are $\Delta H^0(\text{OK})$: -11.63 (reaction 5), -23.19 (reaction 6), -13.09 (reaction 7) kcal/mol.

TABLE 7: G3(MP2) Heats of Formation and Heats of Formation from Isodesmic Reactions at 0 and 298 K (kcal/mol)

molecule	$\Delta H_f^0(0K)$	$\Delta H_f^0(298K)$	$\Delta H_f^0(0K)$	$\Delta H_f^0(298K)$
	G3(MP2)	G3(MP2)	isodesmic	isodesmic
NH ₃	-8.3	-10.0		
trans-N ₂ H ₂	50.7	49.0		
N ₂ H ₄	28.8	25.3		
CH ₃ NH ₂	-0.5	-4.1		
CH ₃ NNH	46.9	43.5	44.9	41.5
CH ₃ NNCH ₃	43.2	38.4	40.0	35.3
CH ₃ HNNHCH ₃	31.3	24.7	28.0	21.5

energetics (with respect to reversibility and ease of reaction), suggesting that these types of compounds may be possible to use in a chemical hydrogen storage system.

Acknowledgment. Funding was provided in part by the Department of Energy, Office of Energy Efficiency and Renewable Energy under the Hydrogen Storage Grand Challenge, Solicitation No. DE-PS36-03GO93013. This work was done as part of the Chemical Hydrogen Storage Center. This research was performed in part using the Molecular Science Computing Facility (MSCF) in the William R. Wiley Environmental Molecular Sciences Laboratory, a national scientific user facility sponsored by the U.S. Department of Energy's Office of Biological and Environmental Research and located at the Pacific Northwest National Laboratory. The Pacific Northwest National Laboratory is operated for the Department of Energy by Battelle. David A. Dixon and Anthony J. Arduengo are indebted to the Robert Ramsay and Saxon Endowments (respectively) of the University of Alabama.

Supporting Information Available: Total CCSD(T) energies (E_h) as a function of basis set. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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